

## FIGURE 1

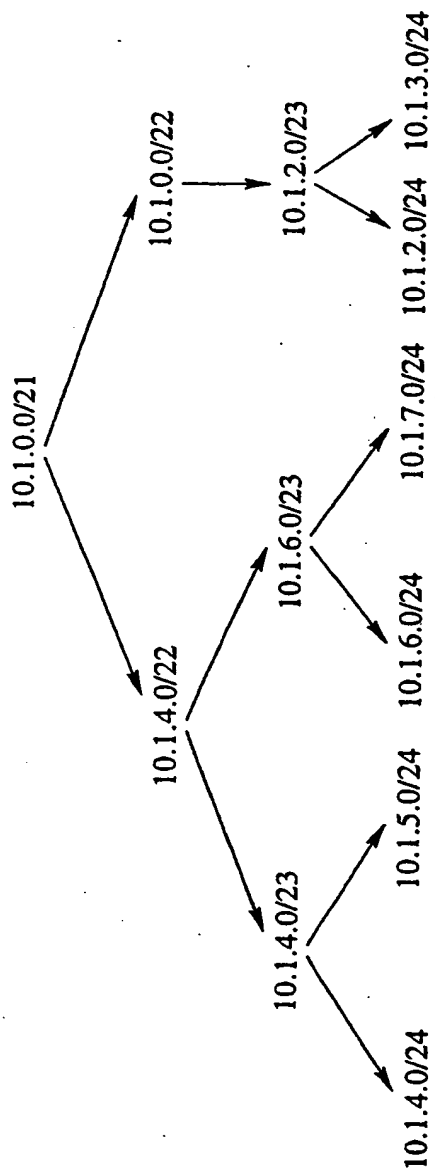


FIGURE 2

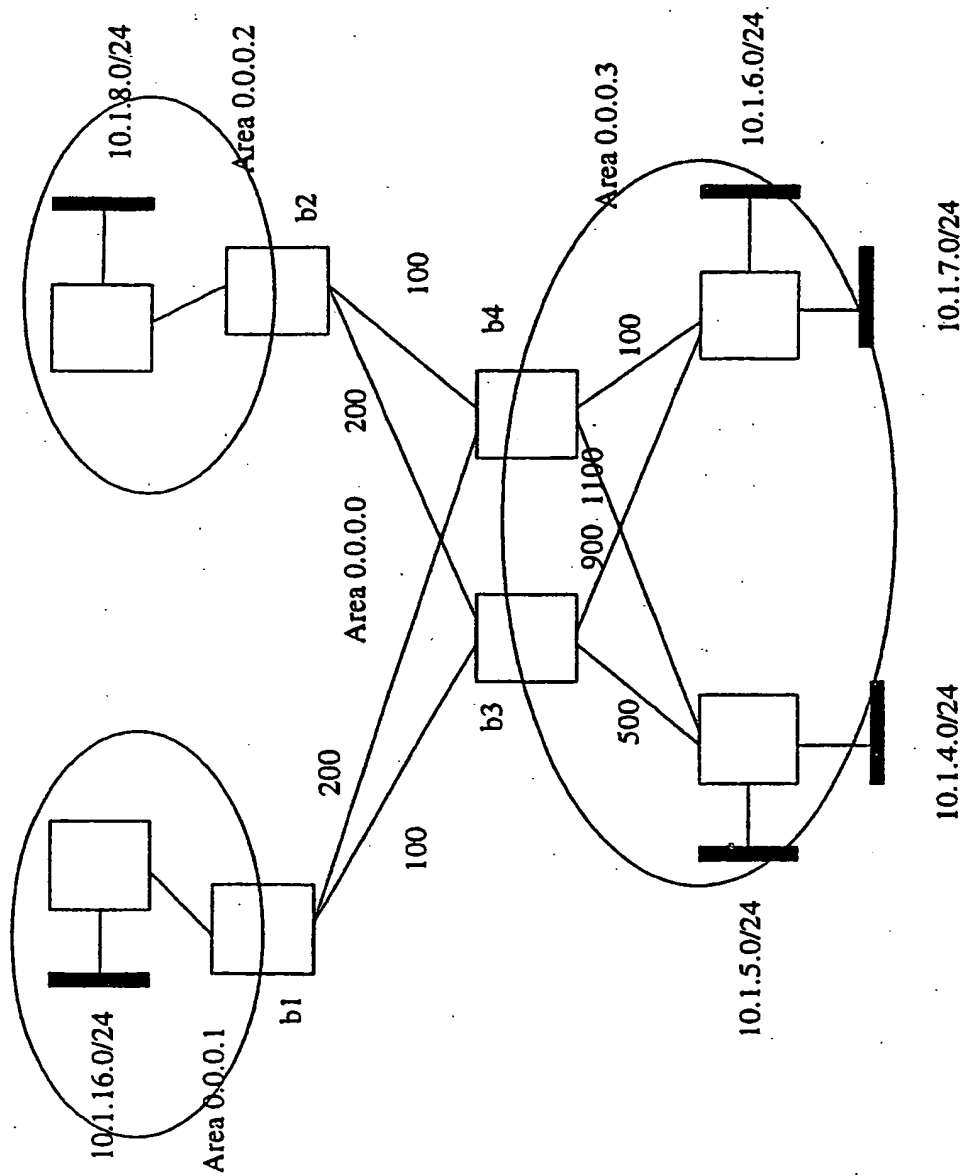
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procedure COMPUTEMINERROR(Aggregate  $x$ , Aggregate  $y$ , integer  $l$ )
1. if subTree[ $x$ ,  $y$ ,  $l$ ].computed = true
2.   return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]
3. minError := minError1 := minError2 :=  $\infty$ 
4. if  $x$  is a leaf {
5.   minError1 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{y\}, W_A) - lsp(s, x))$ 
6.   if  $l > 0$ 
7.     minError2 :=  $\sum_{s \in S} D(s, t) * (lsp(s, x, \{x\}, W_A) - lsp(s, x))$ 
8.   if minError1  $\leq$  minError2
9.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1,  $\emptyset$ ]
10.  else
11.    [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2,  $\{x\}$ ]
12. }
13. if  $x$  has a single child  $u$  {
14.   [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $l$ )
15.   if  $l > 0$ 
16.     [minError2, aggregates2] := COMPUTEMINERROR( $u$ ,  $x$ ,  $l - 1$ )
17.   if minError1  $\leq$  minError2
18.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError1, aggregates1]
19.   else
20.     [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError2, aggregates2  $\cup \{x\}$ ]
21. }
22. if  $x$  has children  $u$  and  $v$  {
23.   for  $i := 0$  to  $l$  {
24.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $y$ ,  $i$ )
25.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $y$ ,  $k - i$ )
26.     if minError1 + minError2 < minError
27.       minError := minError1 + minError2
28.       aggregates := aggregates1  $\cup$  aggregates2
29.   }
30.   for  $i := 0$  to  $l - 1$  {
31.     [minError1, aggregates1] := COMPUTEMINERROR( $u$ ,  $x$ ,  $i$ )
32.     [minError2, aggregates2] := COMPUTEMINERROR( $v$ ,  $x$ ,  $k - i - 1$ )
33.     if minError1 + minError2 < minError
34.       minError := minError1 + minError2
35.       aggregates := aggregates1  $\cup$  aggregates2  $\cup \{x\}$ 
36.   }
37.   [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates] := [minError, aggregates]
38. }
39. subTree[ $x$ ,  $y$ ,  $l$ ].computed := true
40. return [subTree[ $x$ ,  $y$ ,  $l$ ].error, subTree[ $x$ ,  $y$ ,  $l$ ].aggregates]

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FIGURE 3





## FIGURE 5

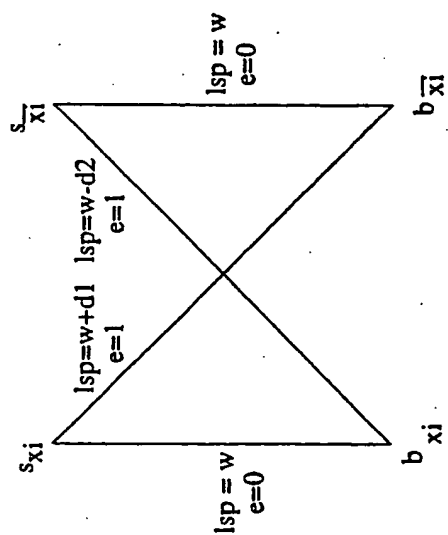
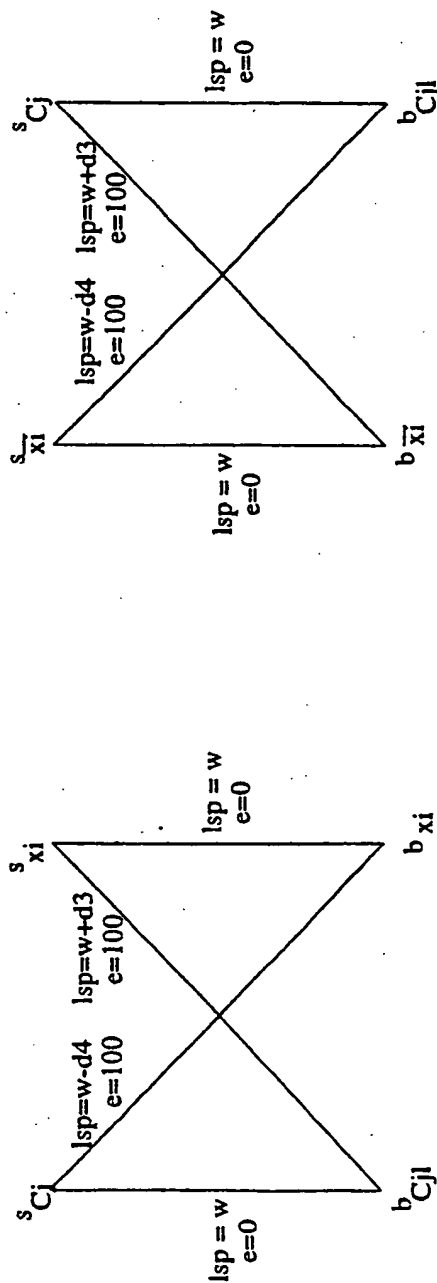


FIGURE 6



(a)  $C_{jl} = x_i$

(b)  $C_{jl} = \bar{x}_i$

FIGURE 7A

FIGURE 7B



**procedure** ComputeWeightsMax(Q)

1. for each  $b \in B_i$  set Wold(b) := 0

2. while (Pb<sub>2</sub>B

i Wold(b) ≤ (

j B<sub>i,j</sub>\*(j B<sub>i,j-1</sub>)

2 ) \*lspmax) f3. Let

Q0 be a new set of inequalities that result when the value Wold(b) is substituted for each variable W (b) only on the LHS of each inequality in Q 4. Set Wnew(b) to the smallest possible value such that each inequality in Q0 is satisfied when Wnew(b) is substituted for variable W (b) in Q0 5. if Wnew = Wold 6. return Wnew 7. else 8. Wold := Wnew 9. g 10. return "there does not exist a weight assignment W "

**FIGURE 9**



1. Set  $V_{opt} := v(s_1)$ ,  $E := E_{opt} := \sum_{s \in S} e(s, b_1)$
2. for  $j := 1$  to  $n$  {
3.      $E := E + e(s_j, b_2) - e(s_j, b_1)$
4.     if  $E < E_{opt}$
5.          $V_{opt} := v(s_{j+1})$ ,  $E_{opt} := E$
6. }

7. return  $V_{opt}$

```

2.  for  $j := 1$  to  $n$  {

```

4. if  $E < E_{opt}$

6. }

```

7. return  $V_{opt}$ 

```

[illegible]